

**DR. BABASAHEB AMBEDKAR TECHNOLOGICAL UNIVERSITY, LONERE –
RAIGAD -402 103
Mid Semester Examination – October - 2017**

Branch: F.Y.B.Tech (Group A/Group B)

Sem.: - I

Subject with Subject Code:- Engineering Mathematics –I (MATH101)

Marks: 20

Date:-03/10/2017

Time:- 1 Hr.

Instructions: - 1. All questions are compulsory.

- 2. Use of nonprogrammable calculator is allowed.**
- 3. Figures to the right indicate full marks.**

(Marks)

Q.No.1 Attempt the following

(06)

- a. The maximum value of the rank of a non-zero matrix $(A)_{4 \times 5}$ is
 - i) 0
 - ii) 1
 - iii) 4
 - iv) 5
- b. If the rank of matrix A is 2, then the rank of matrix A^T is
 - i) 2
 - ii) 0
 - iii) 4
 - iv) 1
- c. The eigen values of a triangular matrix are
 - i) The elements of its principle diagonal
 - ii) 0, 0, 0
 - iii) The elements of its non-principle diagonal
 - iv) none
- d. The two eigen vectors X_1 and X_2 are said to be orthogonal iff
 - i) $X_1 X_2 = I$
 - ii) $X_1 X_2 = 0$
 - iii) $X_1 X_2^T = 0$
 - iv) $X_1^T X_2 = I$
- e. If $y = e^{a \sin^{-1} x}$, then the value of $(1 - x^2)y_2 - xy_1 - a^2y$ is
 - i) 1
 - ii) a
 - iii) 0
 - iv) none

f. The Maclaurin's series of $\tan^{-1} x$ is

- i) $x + \frac{x^3}{3} + \frac{x^5}{5} + \dots$
- ii) $x - \frac{x^3}{3} + \frac{x^5}{5} - \dots$
- iii) $1 - x + x^2 - \dots$...
- iv) $1 + x + x^2 + \dots$...



Q.No. 2 Attempt any one of the following:

(06)

a. Find the eigen values and the corresponding eigenvectors for the Matrix

$$A = \begin{bmatrix} 5 & 0 & 1 \\ 0 & -2 & 0 \\ 1 & 0 & 5 \end{bmatrix}$$

b. If $y = (\sin^{-1} x)^2$, then prove $(1 - x^2)y_{n+2} - (2n + 1)xy_{n+1} - n^2y_n = 0$, and hence prove that $(\sin^{-1} x)^2 = 2 \frac{x^2}{2!} + 2 \cdot 2^2 \frac{x^4}{4!} + 2 \cdot 2^2 \cdot 4^2 \frac{x^6}{6!} + \dots$

Q.No 3. Attempt any two of the following (08)

a. Find for what value of k the set of equations

$$2x - 3y + 6z - 5t = 3, \quad y - 4z + t = 1, \quad 4x - 5y + 8z - 9t = k$$

has (i) no solution (ii) Infinite number of solutions.

b. If $\cos^{-1} \left(\frac{y}{b} \right) = \log \left(\frac{x}{n} \right)^n$, then show that

$$(x^2)y_{n+2} + (2n + 1)xy_{n+1} + 2n^2y_n = 0.$$

c. Find the approximate value of $\tan^{-1}(1.003)$ correct upto four decimal places by using Taylor's theorem.

